

Unit

1

The Solid State

Packing efficiency-Simple cubic:

In simple cubic unit cell, particles meet along edges,

If 'a' is edge length of the unit cell,

'r' is radius of sphere

$$a = 2r$$

$$\text{No of particles in simple cube} = 8 \times \frac{1}{8} = 1$$

$$\text{Packing efficiency} = \frac{\text{No. of particles} \times \text{volume of sphere}}{\text{Total volume of unit cell}} \times 100$$

$$= \frac{1 \times \frac{4}{3} \pi r^3}{(2r)^3} = 52.4\%$$

$$\text{Void space} = 100 - 52.4 = 47.6 \%$$

Calculations involving unit cell dimensions:

If 'a' is the edge length,

'Z' is the no of particles

'm' is mass of an atom

$$\text{Density of the unit cell } (\rho) = \frac{\text{Mass of the unit cell}}{\text{Volume of unit cell}} = \frac{m}{v}$$

$$m = \frac{ZM}{N_A} \text{ (M is molar mass)}$$

$$v = a^3$$

$$\Rightarrow \text{Density, } \rho = \frac{ZM}{a^3 \cdot N_A}$$

