

Chapter 1

Sets

Addition theorem:

1. For two sets A and B.

$$n(A \cup B) = n(A) + n(B) - n(A \cap B).$$

2. $n(A^c \cap B^c) = n(S) - n(A \cup B).$

3. For three sets A, B, C,

$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(C \cap A) + n(A \cap B \cap C)$$

4. $n(A^c \cap B^c \cap C^c) = n(S) - n(A \cup B \cup C).$

Disjoint sets:

Two sets A and B are said to be disjoint.

If $A \cap B = \phi$

Ex. If $A = \{1, 2, 3\}$; $B = \{p, q\}$ then $A \cap B = \phi$; A, B are disjoint sets.

Symmetric difference of two sets:

If A and B are two sets then $(A - B) \cup (B - A)$ is called the Symmetric difference of A and B.

It is denoted by $A \Delta B$, read as A delta B.

$$\begin{aligned} A \Delta B &= (A - B) \cup (B - A) \\ &= \{x : x \in A \text{ or } B \text{ but } x \notin A \cap B\} \end{aligned}$$

Note:

1. $A \Delta B = (A - B) \cup (B - A)$

2. $A \Delta A = \phi$

3. $A \Delta \phi = \Delta$

4. $A \Delta B = \phi \Rightarrow A = B$

