

CHAPTER 11

Areas

Parallelograms on the same base and between the same parallels:

In this section, we shall find a relation between the areas of two parallelograms on the same base and between the same parallel. For this, let us first define the following.

Base:

A base of a parallelogram is any side of it.

Altitude:

For each base of a parallelogram, the corresponding altitude is the line segment from a point on the base, perpendicular to the line containing the opposite side.

Theorem 1:

Parallelograms on the same base and between the same parallels are equal in area.

Given:

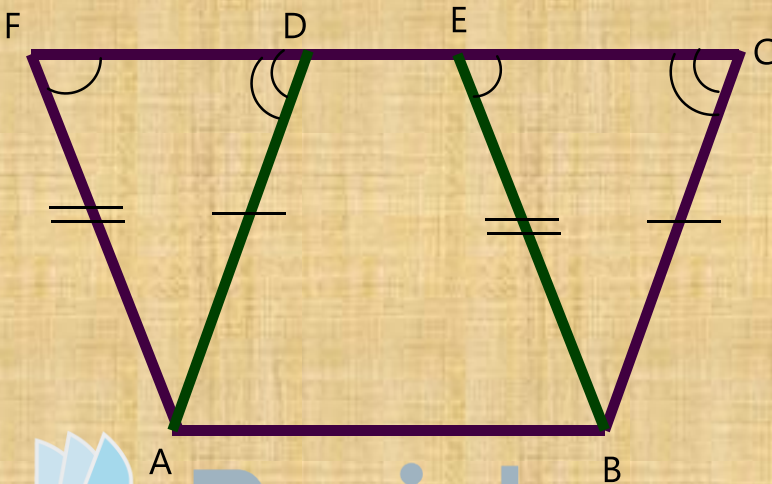
Two parallelograms ABCD and ABEF, which have the same base AB and which are between the same parallel lines AB and FC.

To prove:

$$\text{ar (Parallelogram ABCD)} = \text{ar (Parallelogram ABEF)}$$

Proof:

In $\triangle ADF$ and $\triangle BCE$, we have



$$AD = BC \quad (\because ABCD \text{ is a parallelogram})$$

$$AF = BE \quad (\because ABEF \text{ is a parallelogram})$$

$$\text{And } \angle DAF = \angle CBE$$

$$(\because AF \parallel BE \Rightarrow \angle AFD = \angle BEC \text{ also, } AD \parallel BC \Rightarrow \angle ADF = \angle BCE)$$

By SAS criterion of congruence, we have

$$\triangle ADF \cong \triangle BCE$$

Consider,

$$\text{ar (Parallelogram ABCD)} = \text{ar}(\triangle ABED) + \text{ar}(\triangle BCE)$$

$$= \text{ar} (\triangle ABED) + \text{ar} (\triangle ADF)$$

$$= \text{ar} (\text{Parallelogram ABEF})$$

